

Mathematics

List of possible questions (10 will be selected from each group):

1a: Give the main operators of Boolean algebra.

1b: List the main number sets used in mathematical analysis.

1c: Give the main operations with number sets.

2a: What is transpose matrix, identity matrix and inverse matrix?

2b: Explain the matrix multiplication.

2c: Explain the rule of Sarrus for determinants evaluation.

3a: Explain three situations in the solution of linear equations systems (depending on the relationship between the number of unknowns and number of equations).

3b: Explain the Cramer's rule for the solution of linear equations systems.

3c: Explain the Gaussian elimination method for the solution of linear equations systems.

4a: Explain the basic features of the Cartesian coordinate system.

4b: Explain the basic features of the cylindrical coordinate system.

4c: Explain the basic features of the spherical coordinate system.

5a: Explain the scalar multiplication (product) of two vectors.

5b: Explain the vector multiplication (product) of two vectors.

5c: Explain the mixed multiplication (product) of two vectors.

6a: Explain the monotonicity of a function.

6b: Explain the various extremes of a function.

6c: Explain difference between even and odd functions.

7a: Plot examples of basic polynomial, exponential and logarithm functions.

7b: Plot examples of basic trigonometric functions (with their inverse variants).

7c: Plot examples of basic hyperbolic functions (with their inverse variants).

- 8a: Describe what is a limit of a continuous function.
- 8b: Explain the 4 basic methods for limits of functions evaluation.
- 8c: What is the difference between sequences and series. What is the difference between arithmetic and geometric sequences (series)?
- 9a: Explain the difference between the Cartesian and goniometric (exponential) form of complex numbers.
- 9b: Explain the n -root evaluation of complex numbers.
- 9c: Give some example of a complex function of real variable.
- 10a: Write the definition of derivative of the function.
- 10b: What is the difference between the Leibniz's and Lagrange's notation of derivatives.
- 10c: List the basic differentiation rules and explain them.
- 11a: Give some examples of the differentiation of exponential functions.
- 11b: Give some examples of the differentiation of trigonometric functions.
- 11c: Give some examples of the differentiation of hyperbolic functions.
- 12a: Explain the Taylor series evaluation.
- 12b: Explain L'Hospital's rule.
- 12c: Explain the role of derivatives in graph course analysis.
- 13a: What is the difference between indefinite and definite integrals.
- 13b: Explain the geometrical meaning of definite integration.
- 13c: Explain the per partes method and substitution rule.
- 14a: List properties of definite integrals (e.g. splitting the interval, ...).
- 14b: What kind of improper definite integrals do you know?
- 14c: Give the formula for the evaluation of the length of a graph of a function.

- 15a: Explain the classification of ordinary differential equations.
- 15b: Describe solution methods for homogeneous ordinary differential equations (1st order).
- 15c: Describe solution methods for non-homogeneous ordinary diff. equations (1st order).
- 16a: What is the difference between partial and total derivative evaluation (for functions of several variables).
- 16b: Define the grad and rot operator (differential operator for functions of several variables).
- 16c: Define the div and Laplacian operator (diff. operator for functions of several variables).
- 17a: Explain the reversing of integration order in double integrals (definite int.) evaluation.
- 17b: List some properties of double integrals (definite integrals).
- 17c: Give some example of area evaluation, using double integrals.
- 18a: List some types of frequency distributions, based on their shape.
- 18b: Explain briefly three basic measures of central tendency (of a distribution).
- 18c: Explain briefly three basic measures of dispersion (of a distribution).
- 19a: Write the formula for correlation coefficient.
- 19b: What is the basic difference between correlation and regression analysis.
- 19c: Explain the basic idea of LSQ-method for linear function fitting.

List of possible exercises (4 will be selected):

1. solve a system of linear equations (three equations with three unknowns),
2. find the product of matrices,
3. calculate a determinant (of a matrix of 6 x 6 elements),
4. evaluate a limit of a selected function,
4. evaluate the Taylor series for a selected function,
5. apply the L'Hospital rule for a selected function limit evaluation,
6. analyze a selected function (extremes definition),
7. calculate selected indefinite integrals,

8. calculate selected definite integrals,
9. solve selected differential equation
10. construct (manually) a histogram for a simple data-set