

# Lecture 2: Mechanics

## Content:

- basic terms and quantities
- velocity and acceleration
- force, moment of force, momentum
- work, power
- mechanical energy
- Newton's laws
- Kepler's laws
- Newton's gravitational law
- free fall, motion in gravitational field

# basic terms and quantities

The general study of the relationships between motion, forces, and energy is called **mechanics**.

**Motion** is the action of changing location or position. Motion may be divided into three basic types - translational, rotational, and oscillatory.

The study of motion without regard to the forces or energies that may be involved is called **kinematics**. It is the simplest branch of mechanics.

The branch of mechanics that deals with both motion and forces together is called **dynamics** and the study of forces in the absence of changes in motion or energy is called **statics**.

# basic terms and quantities

**Point (point mass)** is a mass which doesn't have volume (mass focused into one point),

**body (physical object)** is an identifiable collection of matter, which may be more or less constrained to move together by translation or rotation,

**rigid body** is an idealization of a solid body in which deformation is neglected,

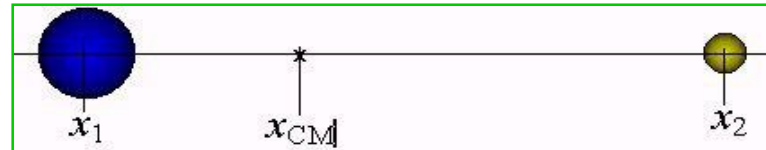
Soft body



Rigid body



**barycentre** is the center of mass of two or more bodies that are orbiting each other,



**trajectory** - path that a moving object follows through space as a function of time.

# basic terms and quantities

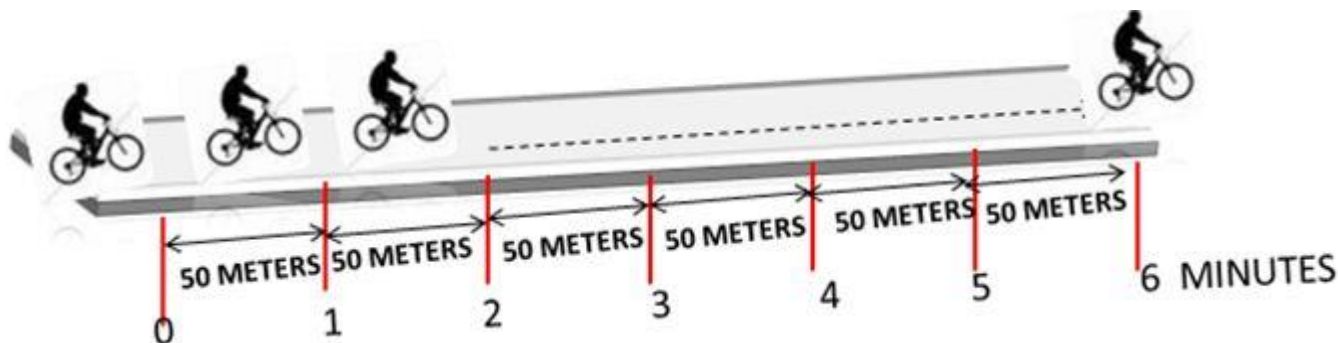
**Velocity (speed):** The velocity  $v$  of an object is the rate of change of its position with respect to a frame of reference, and is a function of time.

It is in general a vector quantity (velocity).

Its size (speed - scalar) can be evaluated:

$$|\vec{v}| = v = \frac{ds}{dt} = s' \quad [\text{m} \cdot \text{s}^{-1}]$$

where  $s$  is path (distance) [m] and  $t$  is time [s].



# basic terms and quantities

**Acceleration:** is the rate of change of velocity of an object.

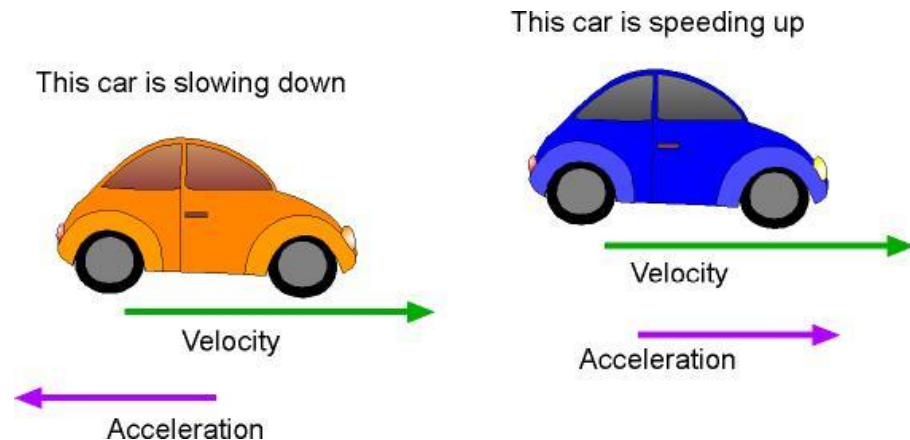
It is in general a vector quantity.

Its size can be evaluated:

$$a = \frac{dv}{dt} = \frac{d^2s}{dt^2} = v' = s'' \left[ \text{m} \cdot \text{s}^{-2} \right]$$

where  $v$  is velocity,  $s$  is path (distance) [m]

and  $t$  is time [s].



# basic terms and quantities

**Angular velocity (speed):** is the rate of change of angular displacement (angle) as a function of time.

It is defined for rotating bodies (because tangential velocity is a function of radius).

It is a vector quantity (pointing in the direction of rotation axis).

Symbol:  $\vec{\omega}$

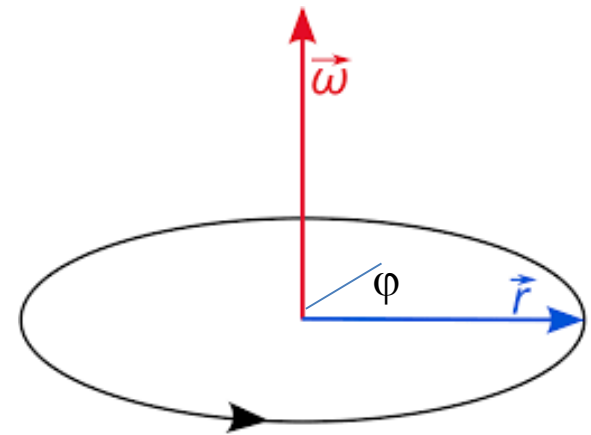
$$|\vec{\omega}| = \frac{d\varphi}{dt}$$

Unit: radians per second [ $\text{rad}\cdot\text{s}^{-1}$ ]

Relationship between angular and tangential velocity:

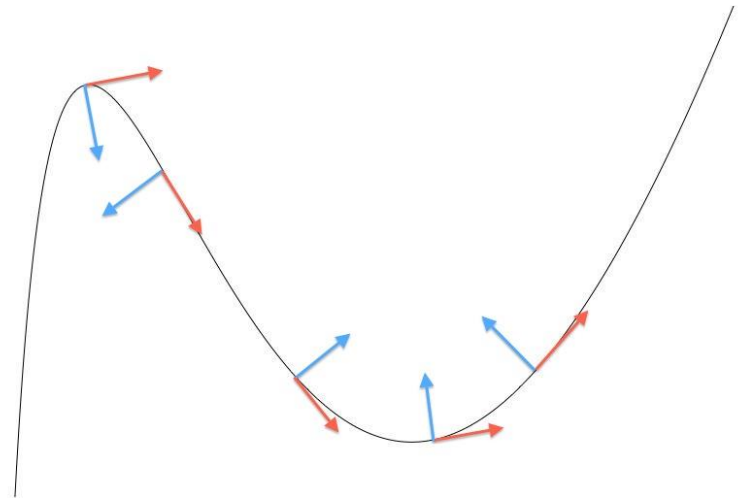
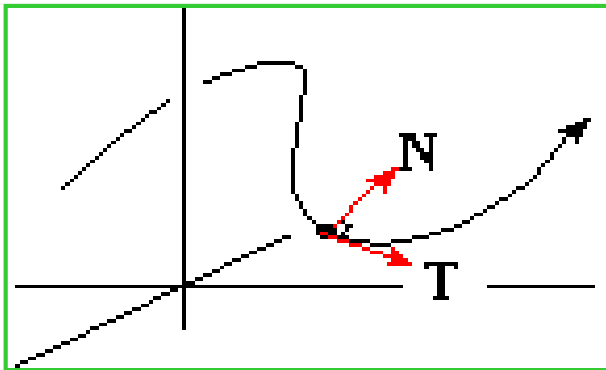
$$|\vec{v}_t| = |\vec{\omega}| r$$

And normal acceleration:  $|\vec{a}_n| = |\vec{\omega}|^2 r$



# Tangent vs normal component

- each vector of velocity and/or acceleration can be split into 2 perpendicular components along a curvilinear path:
- **tangent** component (e.g.  $a_t$ )  
(connected with the change of the vector size)
- **normal** component (e.g.  $a_n$ )  
(connected with the change of vector direction)



# classification of motions

$a_t$	$a_n$	$a$	motion
$a_t = 0$	$a_n = 0$	$a = 0$	uniform straight-line motion; velocity has constant direction and size
$a_t = 0$	$a_n \neq 0$	$a \neq 0$	uniform curvilinear motion; velocity has constant size, but the direction is changed (e.g. motion along a circular line)
$a_t = \text{const.}$	$a_n = 0$	$a \neq 0$	uniformly accelerated, straight-line motion, velocity has the same direction, velocity size is changed
$a_t = \text{const.}$	$a_n \neq 0$	$a \neq 0$	uniformly accelerated, curvilinear motion, velocity direction is changed, velocity size is changed
$a_t \neq \text{const.}$	$a_n = 0$	$a \neq 0$	non-uniformly accelerated, straight-line motion, velocity has the same direction, velocity size is changed
$a_t \neq \text{const.}$	$a_n \neq 0$	$a \neq 0$	non-uniformly accelerated, curvilinear motion, velocity direction is changed, velocity size is changed
		$a = \text{const.}$	motion with constant acceleration (e.g. free fall in Earth gravity field)
$a$ - total acceleration, $a = a_t + a_n$ , $a_t$ - tangent component of acceleration, $a_n$ - normal component of acceleration,			



# basic terms and quantities

## Mass (weight):

Mass is both a *property* of a physical body and a *measure of its resistance* to acceleration (a change in its state of motion) when a force is applied.

- inertial mass measures an object's resistance to being accelerated by a force (represented by the relationship  $F = ma$ ).
- gravitational mass (weight) measures the gravitational force exerted on an object in a known gravitational field.

Comment: Mass of an object should be the same on the Earth and moon, but the weight will be different.

Unit: [kg]

Its definition has to be changed due to the problems with the international prototype.

It is a scalar quantity.

# basic terms and quantities

**Force:** is any interaction that, when unopposed, will change the motion of an object (Galileo). It will change its acceleration and velocity (Newton).

If the mass of the object is constant, this law implies that the acceleration of an object is directly proportional to the force acting on the object (in the direction of the force).

Its size can be evaluated (2. Newton's law):

$$\vec{F} = m\vec{a} \quad [\text{kg} \cdot \text{m} \cdot \text{s}^{-2}] = [\text{N}]$$

where  $m$  is mass [kg] and  $\mathbf{a}$  is acceleration [ $\text{m} \cdot \text{s}^{-2}$ ].  
It is a vector quantity.

# basic terms and quantities

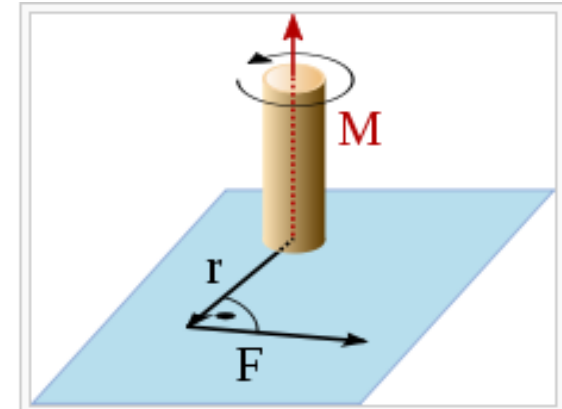
**Moment of force:** is the product of a force and its distance from an axis, which measures the rotation effect of the force (about that axis).

In general it is a combination of a physical quantity and a distance.

$$\vec{M} = \vec{F} \times \vec{r} \quad [\text{N} \cdot \text{m}] = [\text{kg} \cdot \text{m}^2 \cdot \text{s}^{-2}]$$

where **F** is force [N] and  
**r** is distance vector [m].

It is in general a vector quantity.



# basic terms and quantities

**Momentum:** is the product of the mass and velocity of an object. It is connected with the kinematic energy of the moving object.

It is in general a vector quantity.

$$\vec{p} = m\vec{v} \quad [\text{kg} \cdot \text{m} \cdot \text{s}^{-1}]$$



where  $m$  is mass [kg] and  $\mathbf{v}$  is velocity [ $\text{m} \cdot \text{s}^{-1}$ ].



$\neq$



# basic terms and quantities

**Pressure:** Pressure is the amount of force acting per unit area.

$$p = \frac{|\vec{F}|}{s} = \frac{F}{s}$$

where  $F$  is the size of normal force [N] and  $s$  is the area of the surface on contact [m<sup>2</sup>].

Unit is pascal [Pa] = [N/m<sup>2</sup>] = [kg·s<sup>-2</sup>·m<sup>-1</sup>].

Old unit was bar (1 bar = 100000 Pa).

It is in a scalar quantity.

Joke: Newton, Laplace and Pascal play hide-and-go-seek. Laplace starts to count, Pascal jumps behind a bush, but Newton stays on his original place and plots around him with a stick a small square into the soil. Laplace stops to count, see immediately Newton and screams “Newton”! But Newton answers: “No, no my dear friend, what you see is a Newton over m squared – and this is Pascal !!!”.

# basic terms and quantities

## Mechanical work:

In mechanics, a force is said to do work  $W$  if, when acting on a body, there is a displacement of the point of application in the direction of the force.

Its size is given by the product of force and distance.

Unit of work is joule  $[J] = [N \cdot m] = [kg \cdot m^2 \cdot s^{-2}]$ .

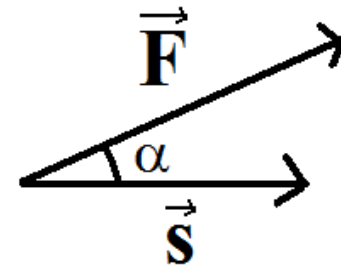
Mathematically it is a scalar product of force and distance (vectors):

$$W = \vec{F} \cdot \vec{s}$$

Size of scalar product is given:

$$W = |\vec{F}| |\vec{s}| \cos \alpha = F s \cos \alpha$$

It is a scalar quantity!



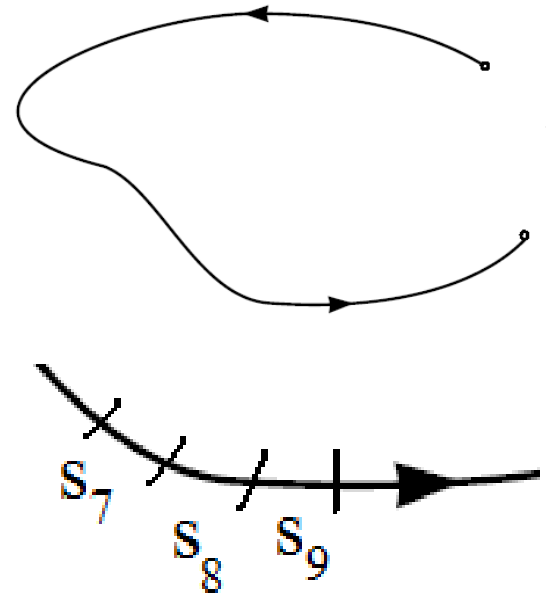
# basic terms and quantities

## Mechanical work:

But what to do, when the trajectory is not straight, but of irregular shape?

We can divide it into  $N$  small parts and evaluate work for each of them:

$$W = \sum_{i=1}^N \vec{F}_i \cdot \vec{s}_i$$



... and when the size of these small parts will be very small...?

$$W = \int_S \vec{F} \cdot d\vec{s} \quad \text{where } \mathbf{S} \text{ is the path and } d\mathbf{s} \text{ its differential.}$$

# basic terms and quantities

## Power:

Power is defined as the rate at which work is done upon an object. Like all rate quantities, power is a time-based quantity.

It is evaluated as the ration of work and time:

$$P = \frac{W}{t}$$

where  $W$  is work [J] and  $t$  is time [s].

Unit of power is watt [W] = [J·s<sup>-1</sup>] = [kg·m<sup>2</sup>·s<sup>-3</sup>].

It is a scalar quantity.



# basic terms and quantities

## **Mechanical energy:**

It is the energy associated with the motion and position of an object:

- kinetic energy ( $E_k$ ),
- potential energy ( $E_p$ ).

In so called conservative fields the sum of potential energy and kinetic energy is constant.

Additional energies in mechanics:

- energy of rotation body,
- elastic energy.

Unit of energy is identical with the unit of mechanical work (joule) [J].

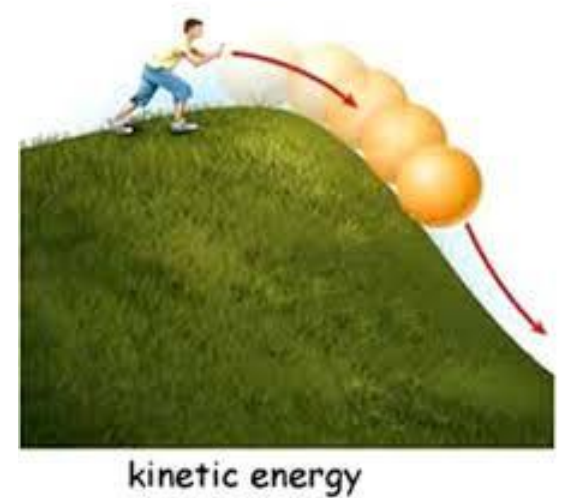
# basic terms and quantities

## Mechanical energy:

**kinetic energy** ( $E_k$ ) - the energy that it possesses due to its motion.

$$E_k = \frac{1}{2}mv^2$$

where  $m$  is the mass [kg] and  
 $v$  the velocity [ $\text{m}\cdot\text{s}^{-1}$ ].



This is valid in classical mechanics.

In relativistic mechanics, this is a good approximation only when  $v$  is much less than the speed of light.

# kinetic energy - derivation:

Energy is connected with work:  $\Delta E = F \Delta s$

for:  $F = ma$   $\Delta s \approx v \Delta t$

is valid:  $\Delta E \approx m a v \Delta t$

and:  $a \Delta t = \Delta v$

is valid:  $\Delta E \approx m v \Delta v$

But where we got the  $\frac{1}{2}$  in the result?:

$$\Delta(v^2) = (v + \Delta v)^2 - v^2 = 2v\Delta v + (\Delta v)^2 \approx 2v\Delta v \Rightarrow v\Delta v = \frac{1}{2} \Delta(v^2)$$

We have ignored the term  $(\Delta v)^2$ , because it is a very small number (e.g.  $0.01^2 = 0.0001$ ).

Final expression:

$$\Delta E \approx \frac{1}{2} m \Delta(v^2) = \Delta\left(\frac{1}{2} m v^2\right)$$

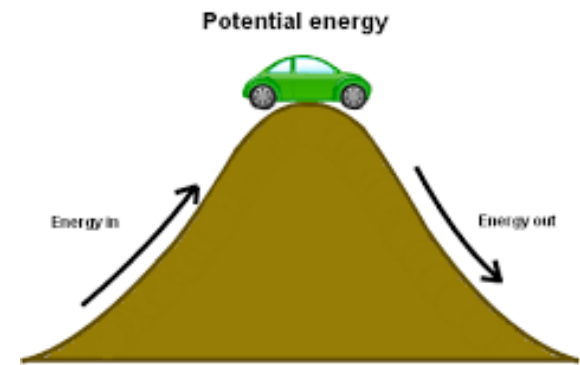
# basic terms and quantities

## Mechanical energy:

**potential energy** ( $E_p$ ) - the energy that an object has due to its position in a force field (mostly gravitational field).

$$E_p = mgh$$

where  $m$  is the mass [kg],  
 $g$  the gravitational acceleration [ $\text{m}\cdot\text{s}^{-2}$ ]  
and  $h$  the height [m].



The change of potential energy is dependent only from the height difference between two points and not from the trajectory of the motion between them.

# basic terms and quantities

**Moment of inertia:** is a measure of an object's resistance to changes in the rotation direction.

For a point mass it can be expressed as:

$$I = mr^2 \quad [\text{kg} \cdot \text{m}^2]$$

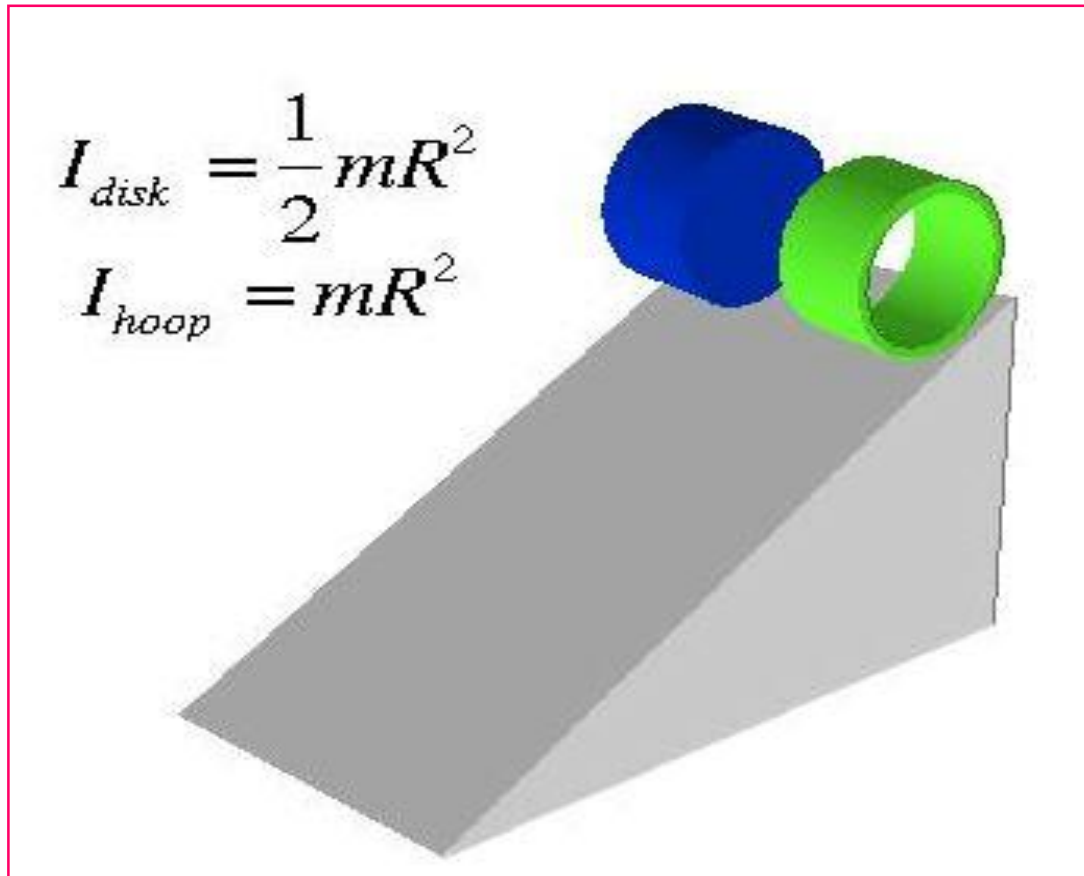
where  $r$  is the distance of the point mass from the rotation axis.

**Energy of rotating body:**

$$E_r = \frac{1}{2} I \omega^2$$

where  $\omega$  is the size of angular velocity.

# Energy of rotating body: a trial



$$E_r = \frac{1}{2}I\omega^2$$

$$I = mr^2$$



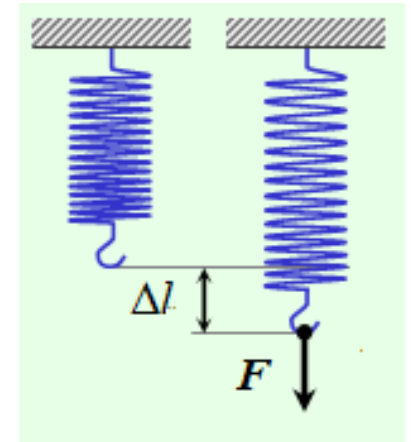
- a) identical masses
- b) different distances of masses from the centre
- c) which one will move faster (will have higher  $\omega$ )?

# basic terms and quantities

## Mechanical energy:

**Elastic energy** ( $E_{El}$ ) - is the potential mechanical energy stored in the configuration of a material or physical system as work is performed to distort its volume or shape. Elastic energy occurs when objects are compressed and stretched, or generally deformed in any manner.

$$E_{El} = \frac{1}{2} k \Delta l^2$$



where  $k$  is so called spring constant and  $\Delta l$  is the length change of the spring.

# Lecture 2: Mechanics

## Content:

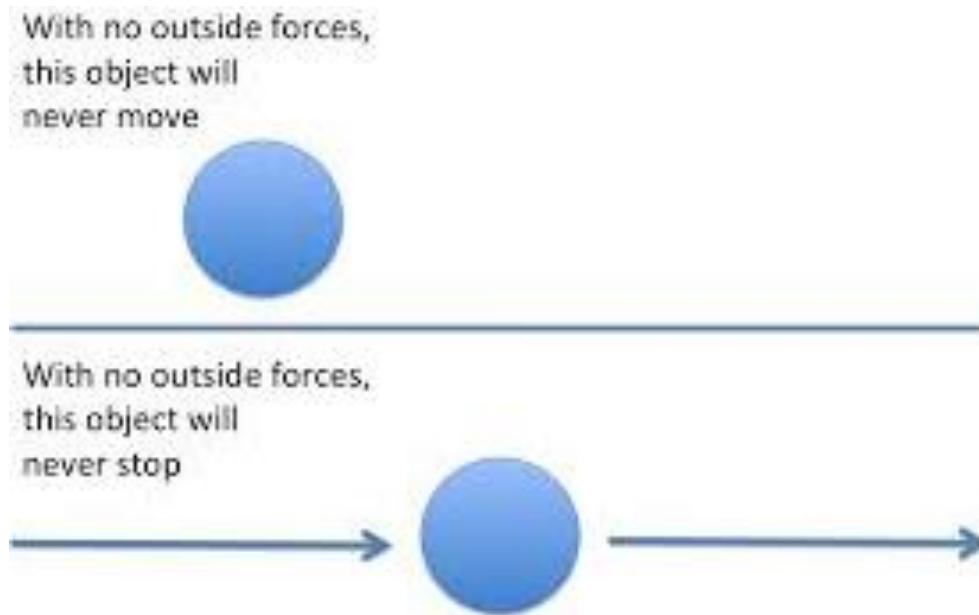
- basic terms and quantities
- velocity and acceleration
- force, moment of force, momentum
- work, power
- mechanical energy
- **Newton's laws**
- **Kepler's laws**
- **Newton's gravitational law**
- **free fall, motion in gravitational field**



# Newton's **three laws of motion**:

- I. Every object in a state of uniform motion tends to remain in that state of motion unless an external force is applied to it.

This we recognize as essentially Galileo's concept of inertia, and this is often termed simply the "**Law of Inertia**" (inertia is the tendency of matter to resist changes in its velocity).



# Newton's **three laws of motion**:

II. The relationship between an object's mass  $m$ , its acceleration  $\mathbf{a}$ , and the applied force  $\mathbf{F}$  is:  $\mathbf{F} = m\mathbf{a}$  or  $\vec{F} = m\vec{a}$   
Acceleration and force are vectors; in this law, directions of the both vectors is the same. Simply the "**Law of Power**"

This is the **most powerful of Newton's three Laws**, because it allows quantitative calculations of dynamics: how do velocities change when forces are applied.

Notice the fundamental difference between Newton's 2<sup>nd</sup> Law and the dynamics of Aristotle: **according to Newton, a force causes only a change in velocity (an acceleration); it does not maintain the velocity as Aristotle held.**  
Thus, **according to Aristotle there is only a velocity if there is a force**, but **according to Newton a force acts on it to cause an acceleration** (that is, a change in the velocity).

## Newton's **three laws of motion**:

- II. The relationship between an object's mass  $m$ , its acceleration  $\mathbf{a}$ , and the applied force  $\mathbf{F}$  is:  $\mathbf{F} = m\mathbf{a}$  or  $\vec{F} = m\vec{a}$   
Acceleration and force are vectors; in this law, directions of the both vectors is the same.

Physical quantities and units:

$$[m] = \text{kg}$$

$$[\mathbf{a}] = \text{m} \cdot \text{s}^{-2} \quad (\text{change of velocity with respect to the time})$$

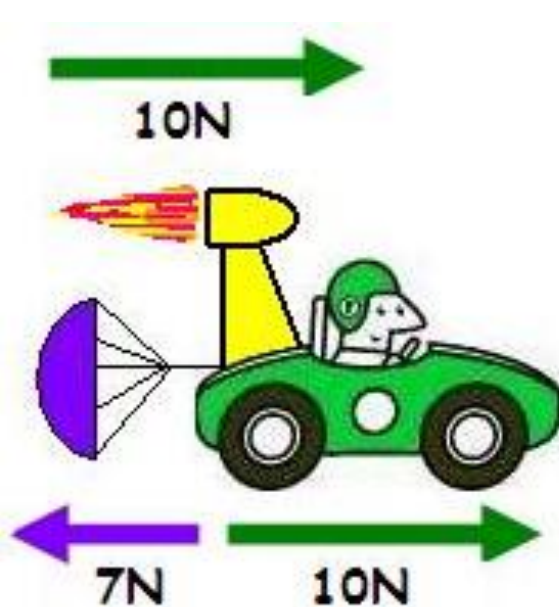
$$[\mathbf{F}] = \text{N} = \text{kg} \cdot \text{m} \cdot \text{s}^{-2}$$

Comment: velocity and acceleration defined by means of derivatives:

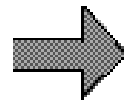
$$v = \frac{ds}{dt} = s' \quad [\text{m} \cdot \text{s}^{-1}] \quad a = \frac{dv}{dt} = \frac{d^2s}{dt^2} = v' = s'' = [\text{m} \cdot \text{s}^{-2}]$$

# Newton's **three laws of motion**:

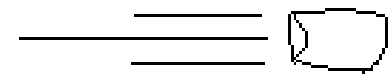
- II. The relationship between an object's mass  $m$ , its acceleration  $\mathbf{a}$ , and the applied force  $\mathbf{F}$  is:  $\mathbf{F} = m\mathbf{a}$  or  $\vec{F} = m\vec{a}$   
Acceleration and force are vectors; in this law, directions of the both vectors is the same.



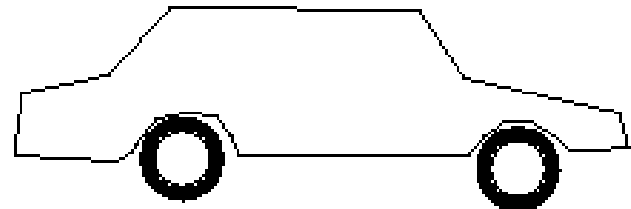
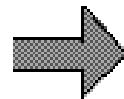
Same force



small mass: large acceleration



large mass: small acceleration



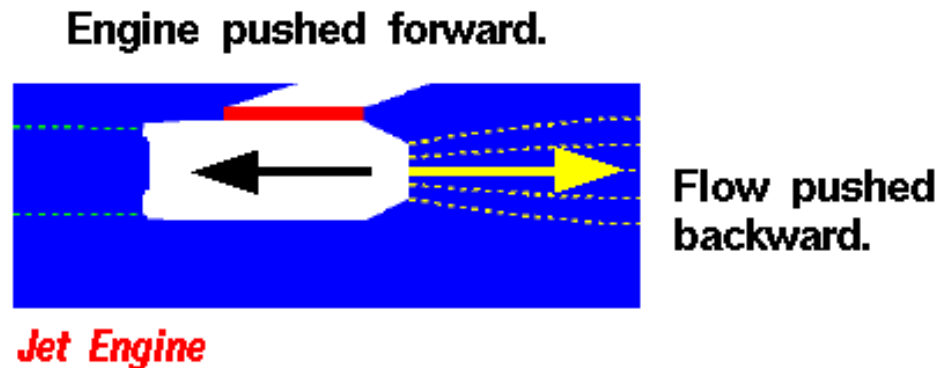
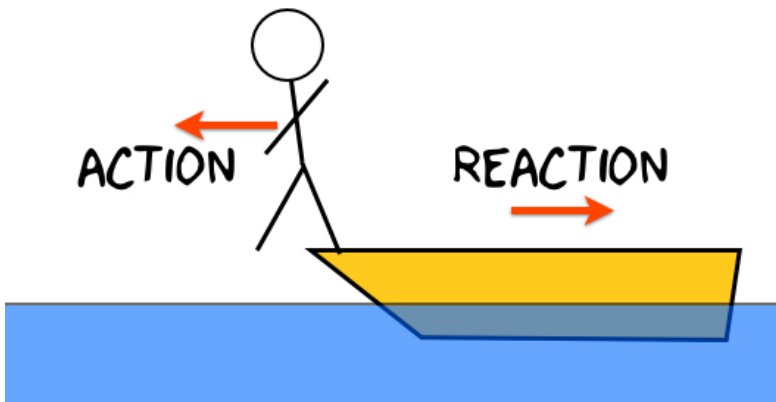
Force = mass x acceleration

# Newton's **three laws of motion**:

III. For every action there is an equal and opposite reaction.

This is often termed simply the "**Law of action and reaction**".

This law is exemplified by what happens if we step off a boat onto the bank of a lake: as we move in the direction of the shore, the boat tends to move in the opposite direction (leaving us facedown in the water, if we aren't careful!).

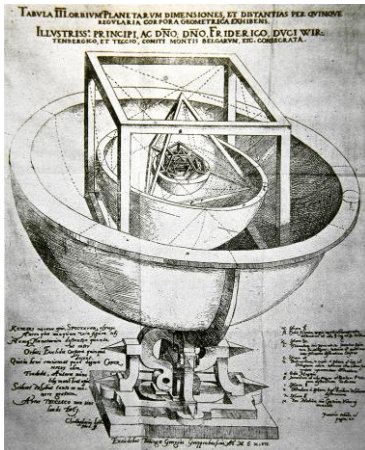


# gravitation



# Kepler's Work

- Tycho Brahe led a team which collected data on the position of the planets (1580-1600 with no telescopes).
- mathematician Johannes Kepler was hired by Brahe to analyze the data.

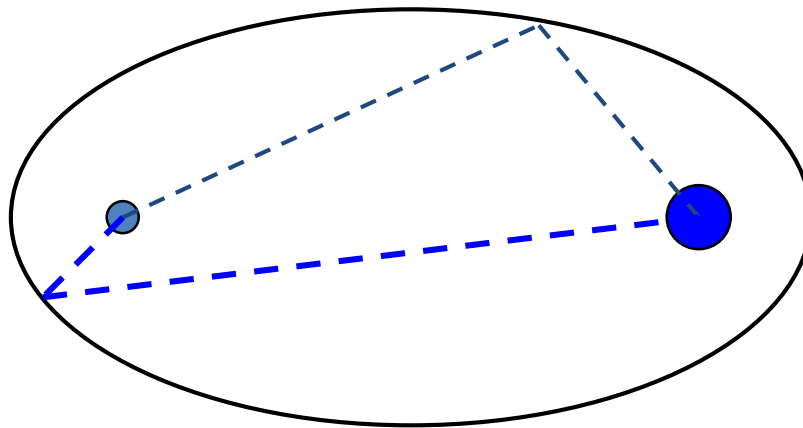


Johannes Kepler  
1571 - 1630

- he took 20 years of data on position and relative distance.
- no calculus, no graph paper, no log tables.
- both Ptolemy and Copernicus were wrong.
- he **determined three laws of planetary motion** (1600-1630).

# Kepler's First Law

- The orbit of a planet is an ellipse with the sun at one focus.

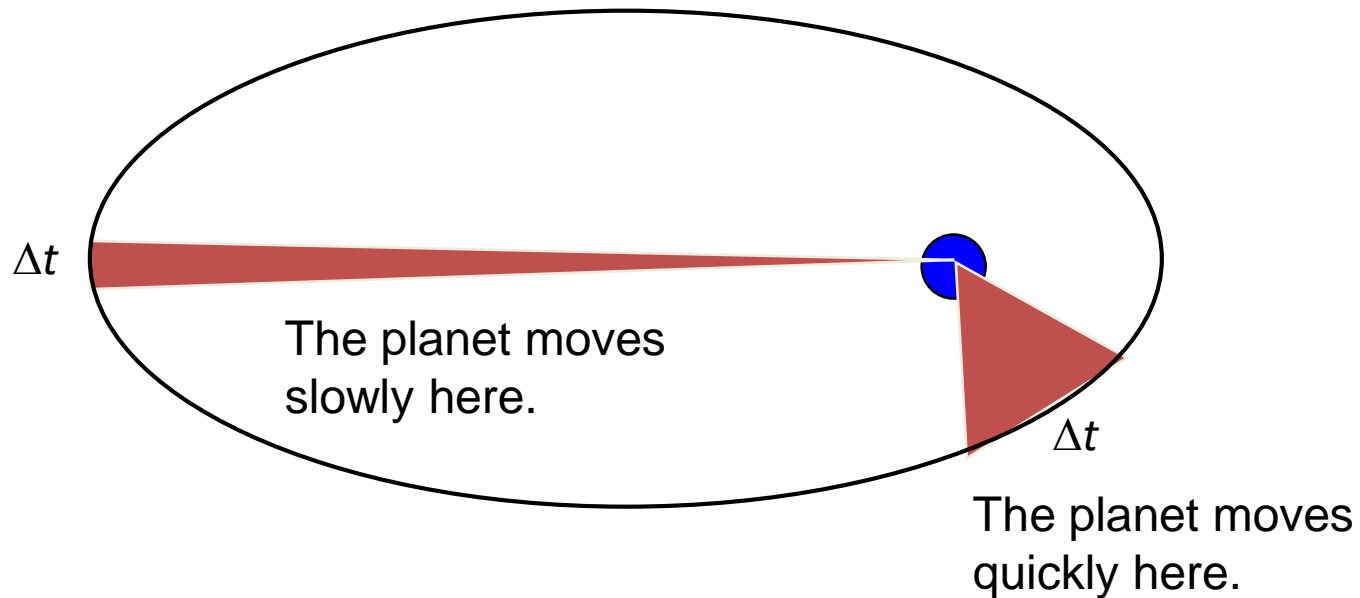


A path connecting the two foci to the ellipse always has the same length.



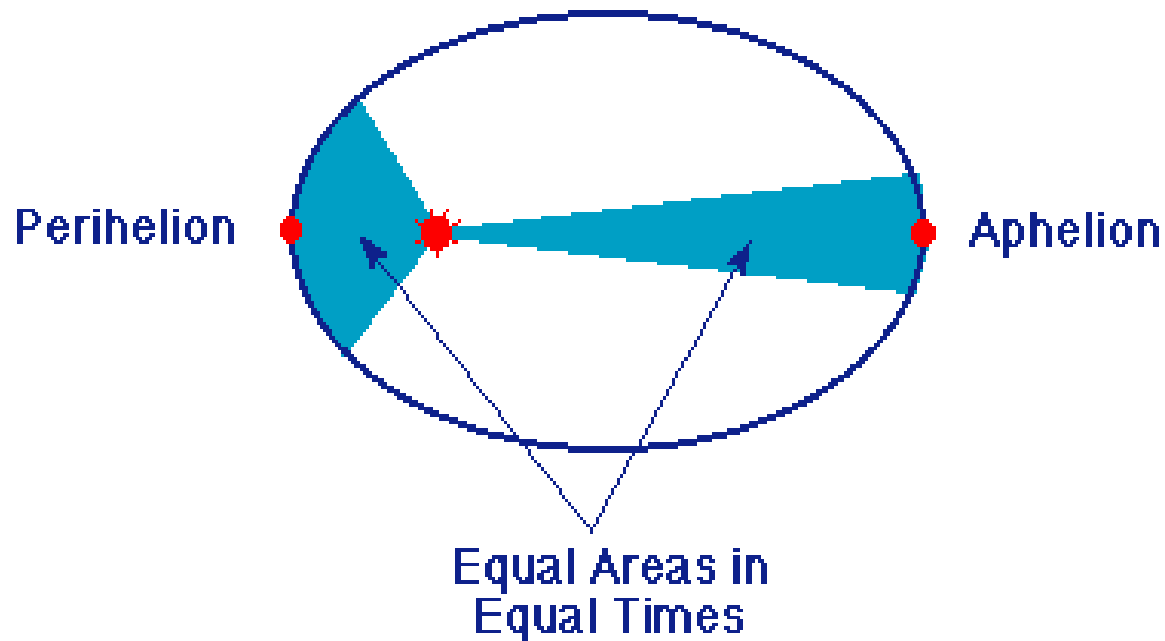
# Kepler's Second Law

- The line joining a planet and the sun sweeps equal areas in equal time.



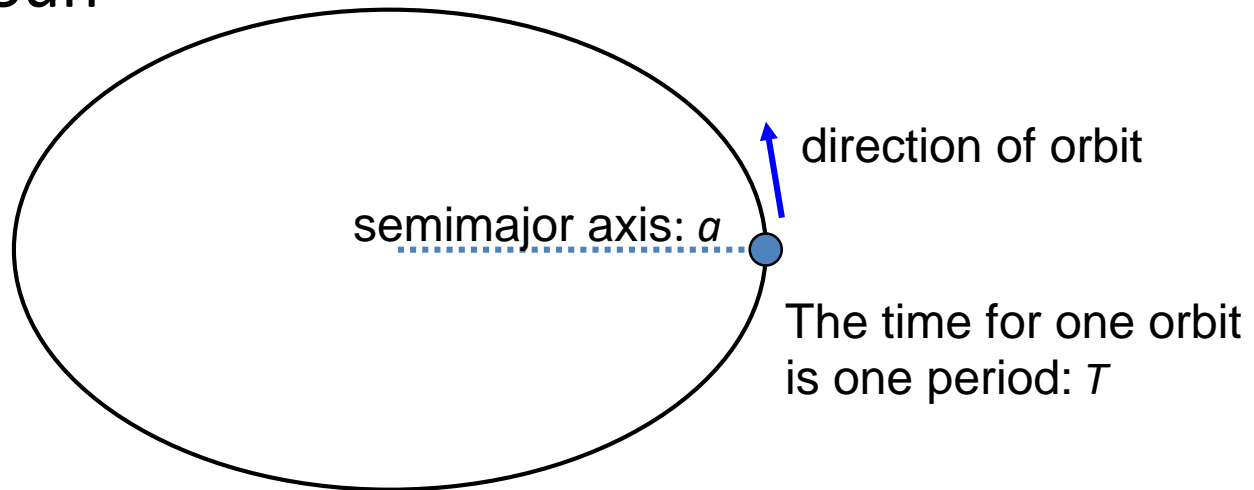
# Kepler's Second Law

- The line joining a planet and the sun sweeps equal areas in equal time.



# Kepler's Third Law

- The square of a planet's period is proportional to the cube of the length of the orbit's semimajor axis.
  - $T^2/a^3 = \text{constant}$
  - The constant is the same for all objects orbiting the Sun



# Kepler's Third Law

**Example:** *planets Earth and Jupiter.*

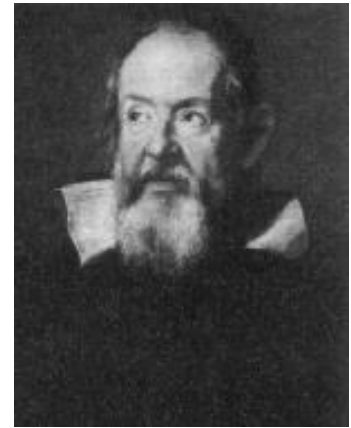
Jupiter's period is **11.86 year** (11,86-times period of Earth),  
semimajor axis (compared to Earth) is **5.2-times** larger.

So, it should be valid:

$$(11.86)^2/1^3 = (5.2)^2/1^3$$
$$140.66 \approx 140.61$$



# Work of Galileo Galilei



Galileo Galilei  
(1564 - 1642)



- various contributions to the concept of modern science,
- mathematical derivations,
- astronomical observations,
- engineering experiments,
- free fall experiments  
(velocity is independent from the body mass  
- a contradiction to Aristotelian physics).

Very nice trial (Brian Cox, vacuum chamber):

<https://www.youtube.com/watch?v=E43-CfukEgs&feature=youtu.be>

Experiment on the Moon (Apollo 15):

[https://upload.wikimedia.org/wikipedia/commons/transcoded/e/e8/Apollo\\_15\\_feather\\_and\\_hammer\\_drop.ogv/Apollo\\_15\\_feather\\_and\\_hammer\\_drop.ogv.240p.webm](https://upload.wikimedia.org/wikipedia/commons/transcoded/e/e8/Apollo_15_feather_and_hammer_drop.ogv/Apollo_15_feather_and_hammer_drop.ogv.240p.webm)

# Newton's Work

- laws of motion
- universal law of gravity
- mathematical derivation of Kepler's laws
- introduction of calculus (derivatives)
- most important work:

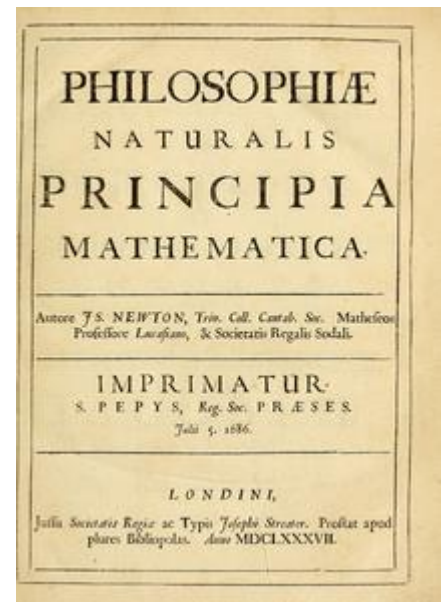
Philosophiæ Naturalis Principia Mathematica  
("Mathematical Principles of Natural Philosophy"),  
first published 5 July 1687

(later edited versions: 1713 and 1726)

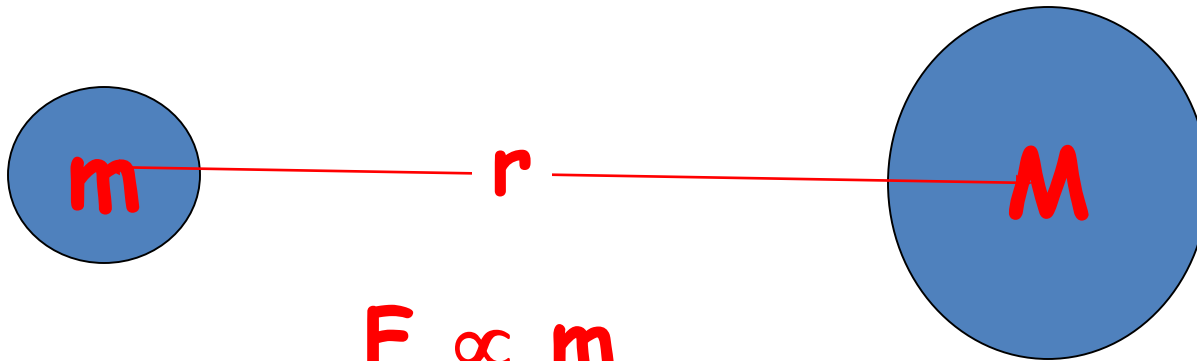
- he spent the second half of his life in Royal mint



Isaac Newton  
1643 - 1727



# Universal law of gravity



$$F \propto m$$

$$F \propto M$$

$$F \propto \frac{1}{r^2}$$

combine:

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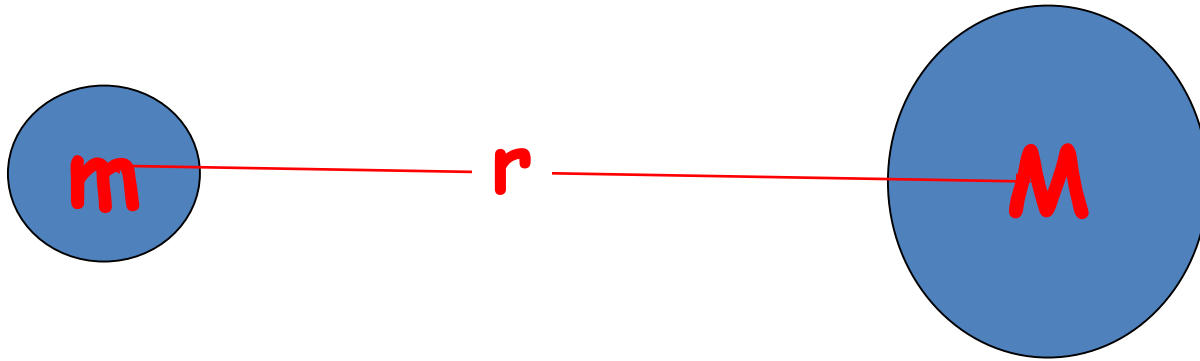
$$F \propto \frac{mM}{r^2}$$

Proportionality constant:

"Newton's Constant"

$$F = G \frac{mM}{r^2}$$

# Universal law of gravity



Newton's law of universal gravitation states that any two bodies in the universe attract each other with a force that is directly proportional to the product of their masses ( $m, M$ ) and inversely proportional to the square of the distance between them ( $r$ ).

$$|\vec{F}_G| = G \frac{mM}{r^2}$$

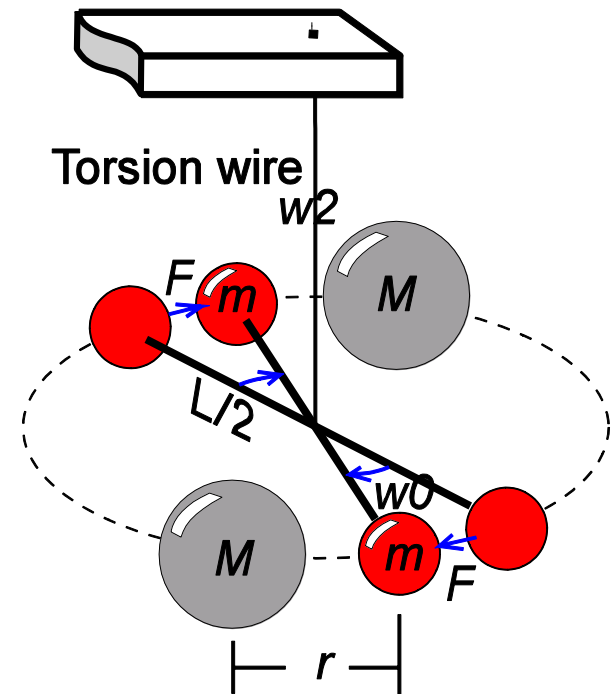
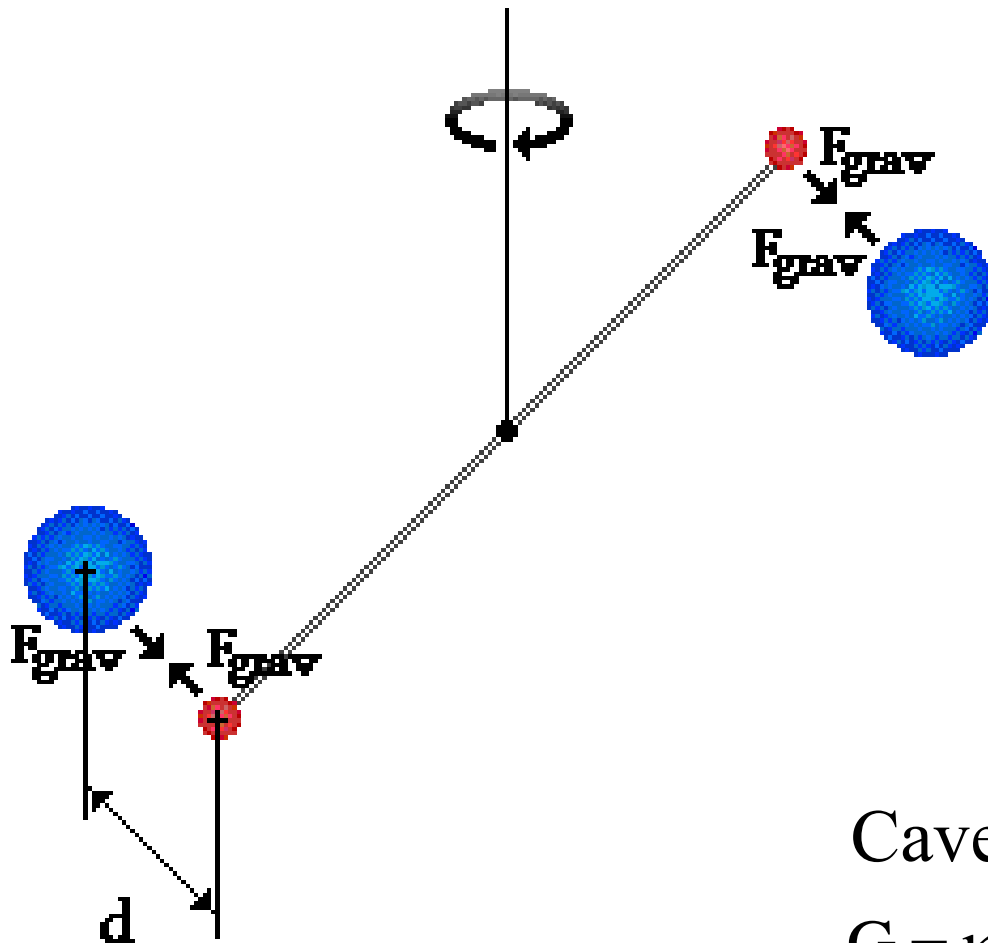
$$G = \kappa = 6.67 \cdot 10^{-11} \left[ \text{N} \cdot \text{m}^2 \cdot \text{kg}^{-2} \right]$$

$G$  – is universal gravitational constant  
(estimated for the first time by H. Cavendish in 1797-1798)



# Measuring gravity force between “ordinary-sized” objects is very hard

## Cavendish's Torsion Balance



Cavendish's value:

$$G = \kappa = 6.74 \cdot 10^{-11} \left[ \text{N} \cdot \text{m}^2 \cdot \text{kg}^{-2} \right]$$

# gravitational acceleration (g):

Newton's gravity law:

$$F = G \frac{mM}{r^2}$$

2. Newton's  
motion law:

$$F = mg \Rightarrow g = \frac{F}{m} \Rightarrow g = G \frac{M}{r^2} \quad [\text{m} \cdot \text{s}^{-2}]$$

## Value of g?

In our country approx.  $9.81 \text{ m} \cdot \text{s}^{-2}$  (rounded  $10 \text{ m} \cdot \text{s}^{-2}$  ).

It is not a constant! Its value is influenced by many factors (rotation of Earth, distance from Earth center, large masses on the surface or below it).

But in the same place on the Earth it acts on falling object independently on their mass (in vacuum).

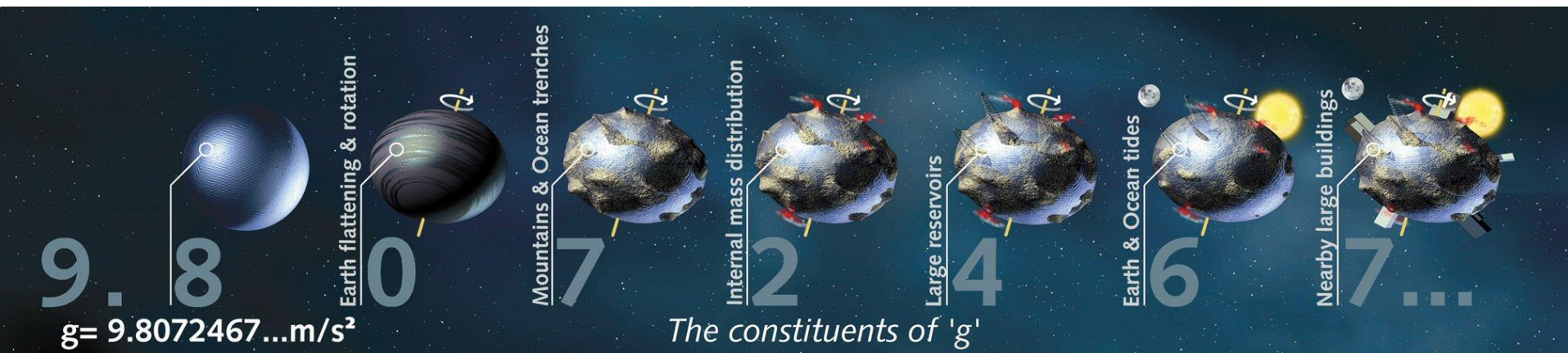
# gravitational acceleration (g):

Estimation of the g value for our Earth:

(mass of the Earth  $\sim 5.97 \cdot 10^{24}$  kg; radius  $\sim 6371000$  m,  
 $G \sim 6.67 \cdot 10^{-11}$  N·m<sup>2</sup>/kg<sup>2</sup>)

$$g = G \frac{M}{r^2} \approx 9.8 \text{ [m} \cdot \text{s}^{-2}\text{]}$$

In one point at the Earth surface g value is constant (independent from the mass), but it changes with the change of position (!)



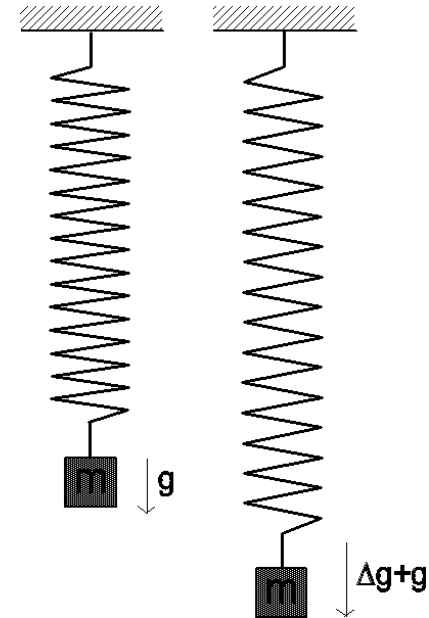
# gravitational acceleration (g) - measurement:



free-fall instrument  
(absolute gravimeter)

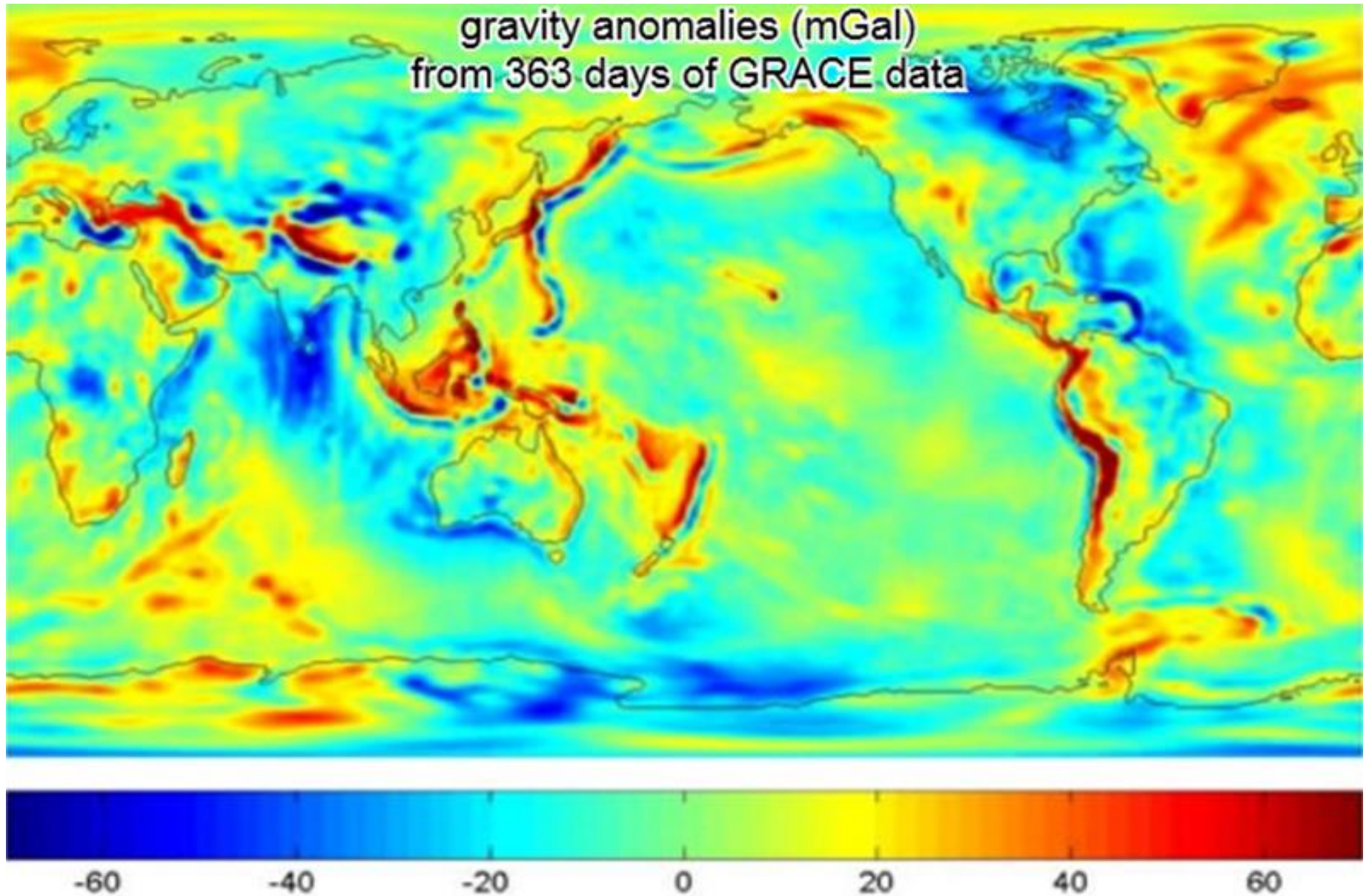


string instrument  
(relative gravimeter)

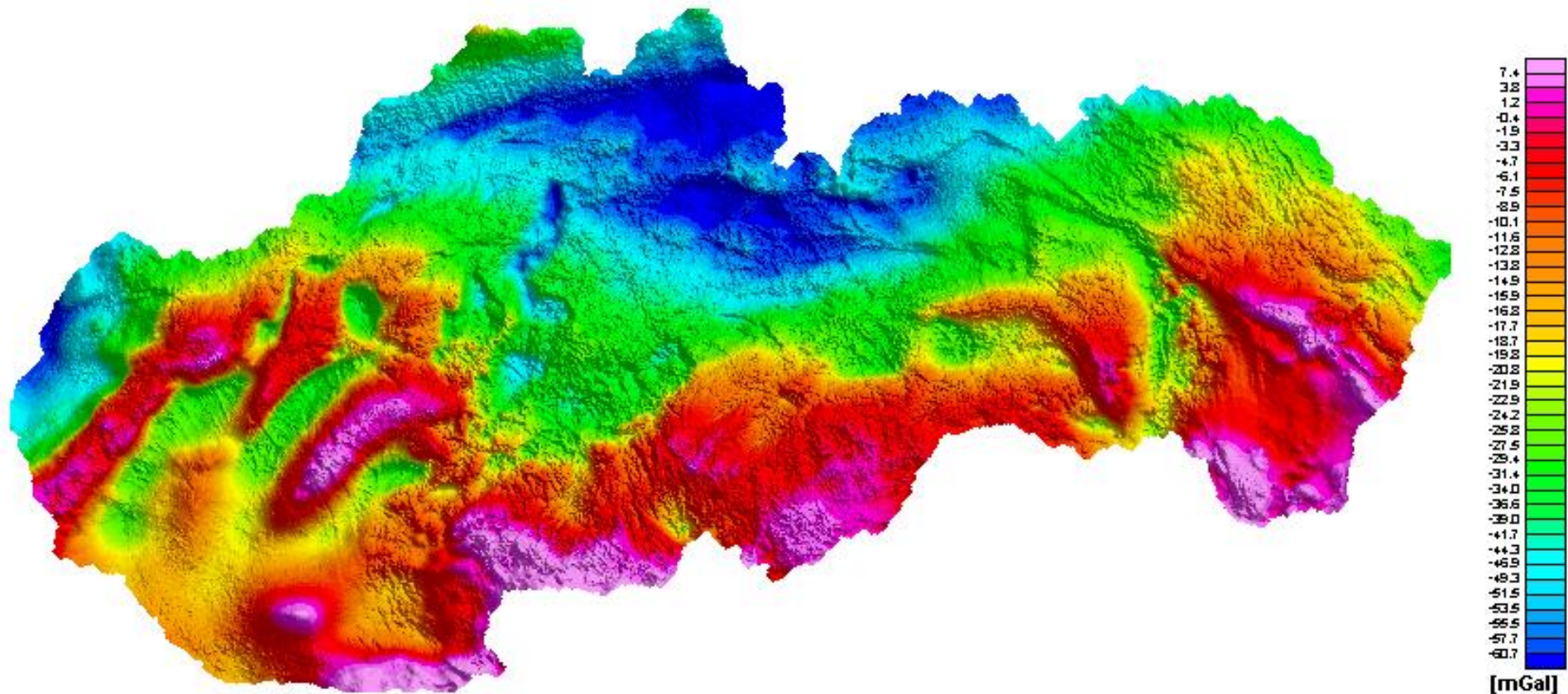




## gravity anomalies - worldwide



# gravity anomalies - Slovakia



# free fall – basic equations (1/2)

From 2. Newton's law of motion it follows:

$$mg = m \frac{\partial^2 s}{\partial t^2}$$

$$g = \frac{\partial^2 s}{\partial t^2}$$

Integrating this equation with respect to t, we get:

$$\int g dt = \int \left[ \frac{\partial^2 s}{\partial t^2} \right] dt$$

$$g \int dt = \frac{\partial s}{\partial t} + c_1$$

$$gt + c_2 = \frac{\partial s}{\partial t} + c_1$$

$$gt = v + c_3$$

$$v = gt + v_0$$

Accepting the original condition that for the time  $t = 0$  the initial velocity of the object at some level  $z_0$  is  $v_0$ , we get:  $c_3 = -v_0$ .

# free fall – basic equations (2/2)

$$v = gt + v_0$$

In further step we integrate this equation again with respect to t:

$$\int v dt = \int [gt + v_0] dt$$

$$s + c_4 = \int gtdt + \int v_0 dt$$

$$s + c_4 = g \int t dt + v_0 \int dt$$

$$s + c_4 = g \frac{t^2}{2} + c_5 + v_0 t + c_6$$

$$s = g \frac{t^2}{2} + v_0 t + c_7$$

$$s = \frac{1}{2}gt^2 + v_0t + z_0$$

Accepting the original condition that for the time  $t = 0$  the position of the object is the level  $z_0$  we get:  $c_7 = z_0$ .



# free fall

$$s = \frac{1}{2}gt^2 + v_0t + z_0$$

When we take the original values for the time  $t = 0$ :  
 $z_0 = 0$  and  $v_0 = 0$ , we get the well known formula:

$$s = \frac{1}{2}gt^2$$

Example:

$$t_1 = 1 \text{ sec} \Rightarrow s_1 = 0.5 g t_1^2 = 5 \cdot 1 = 5 \text{ m}$$

$$t_2 = 2 \text{ sec} \Rightarrow s_2 = 0.5 g t_2^2 = 5 \cdot 4 = 20 \text{ m}$$

$$t_3 = 3 \text{ sec} \Rightarrow s_3 = 0.5 g t_3^2 = 5 \cdot 9 = 45 \text{ m}$$

$$t_4 = 4 \text{ sec} \Rightarrow s_4 = 0.5 g t_4^2 = 5 \cdot 16 = 80 \text{ m}$$



# free fall

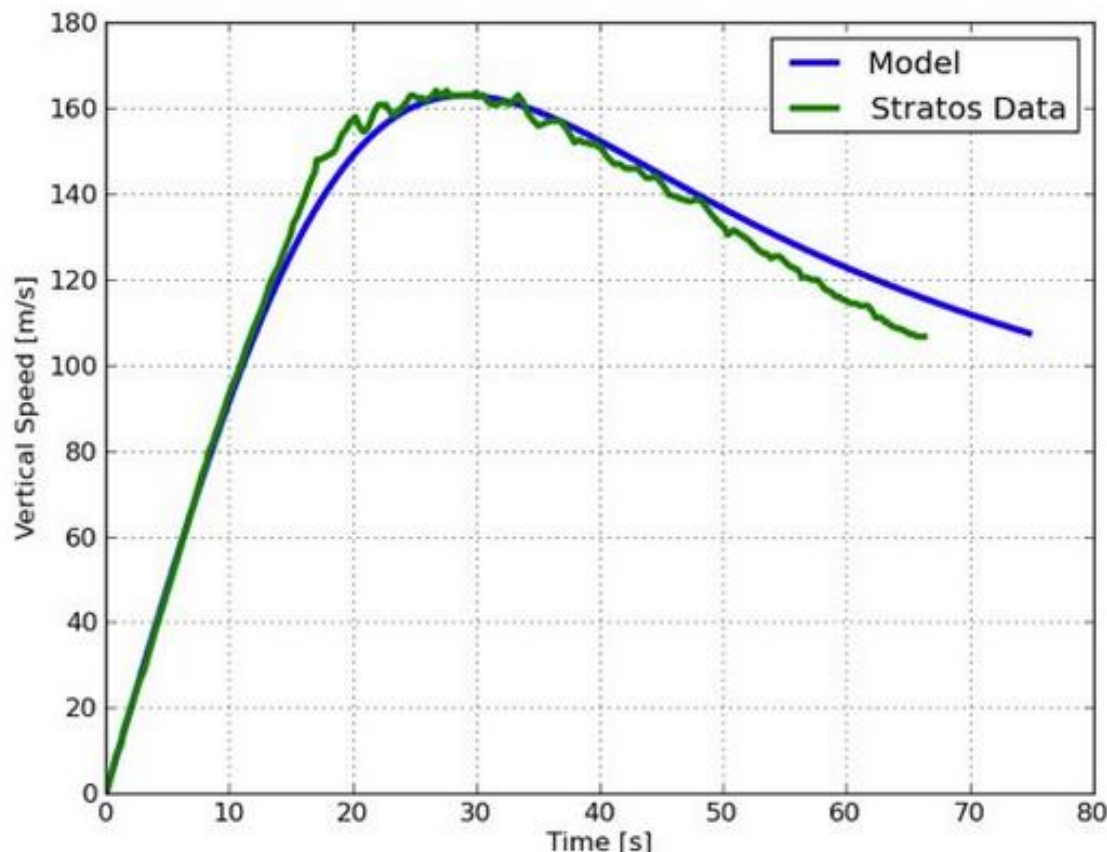
$$s = \frac{1}{2}gt^2 \Rightarrow t = \sqrt{\frac{2s}{g}}$$

Example: jump of Felix Baumgartner (2012)

height: 38 969 m

time: 4 min 20 sec.

Can we check it by means of free fall formula?

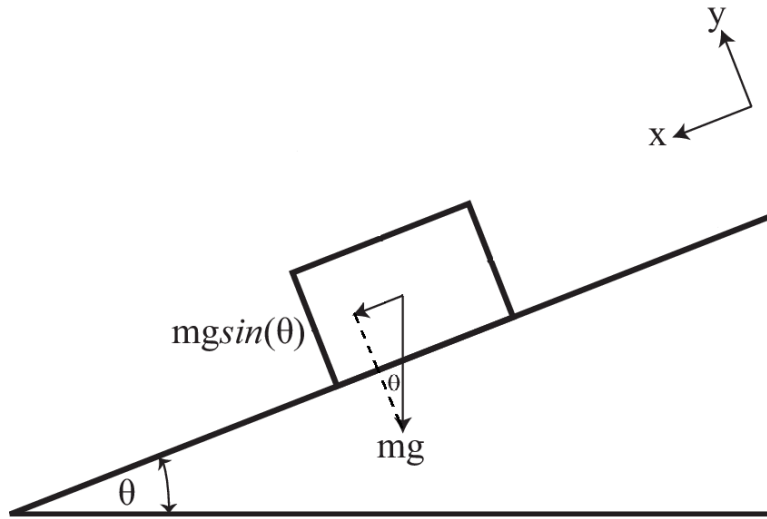


Air resistance:

$$|\vec{F}_{\text{AIR}}| = -k|\vec{v}|^2$$

where  $k$  is the air resistance coefficient  
 $k = 0.24 \text{ [kg/m]}$

# motion along inclined plane



$$\mathbf{F}_G = m\mathbf{g}$$

From the figure it follows:

$$\begin{aligned} \mathbf{a} &= \mathbf{F}_G/m = (\mathbf{F}_G\sin\theta)/m = \\ &= (mg\sin\theta)/m = \mathbf{g}\sin\theta \end{aligned}$$

From this derivation and also from experiments it follows that the accelerated motion along inclined plane is also **independent from the body mass**.

This is valid even in a case that there is a rotation of the moving object (e.g. rolling of a solid sphere).

**[external video](#)**

# motion in gravitational field

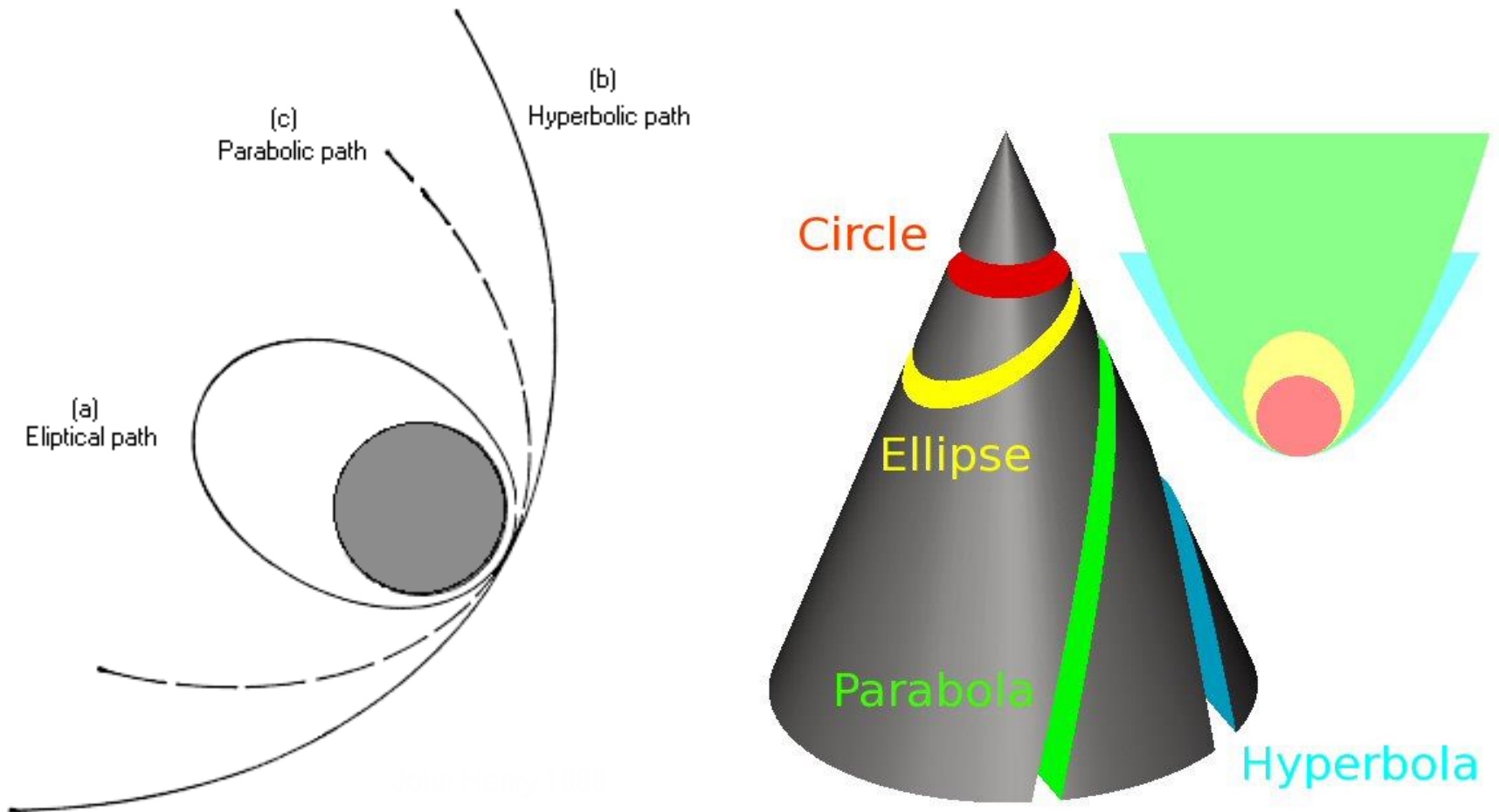


Fig-1: Types of paths

different orbits shapes

# motion in gravitational field

When we move under some angle (not a free fall), equations became little bit more complicated, but they can be solved.



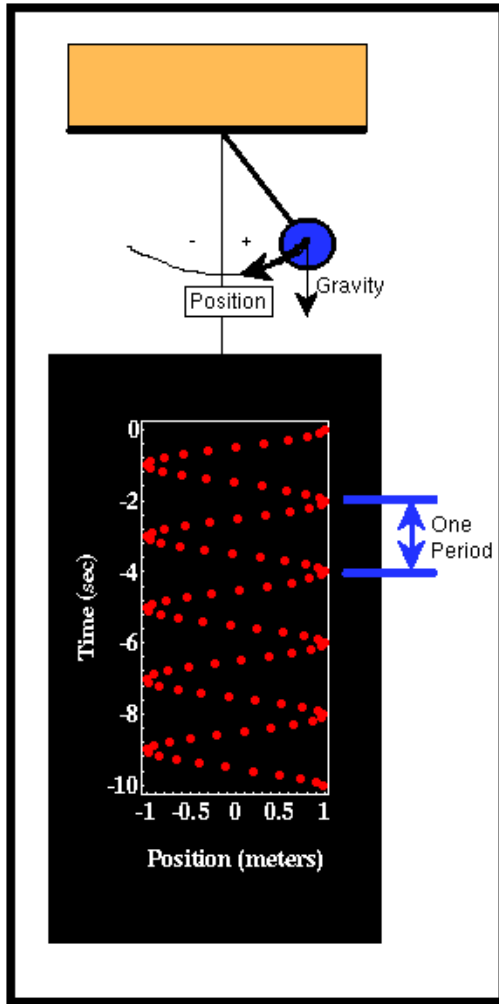
Stroboscopic shoots of a moving ball that trajectory have shapes of parabolas (in fact parts of ellipses)

period of a mathematic pendulum (T):

Is also independent on the mass of the object,  
it is a function of the length  $l$  and gravitational  
acceleration  $g$ :

$$T = 2\pi \sqrt{\frac{l}{g}} \text{ [s]}$$

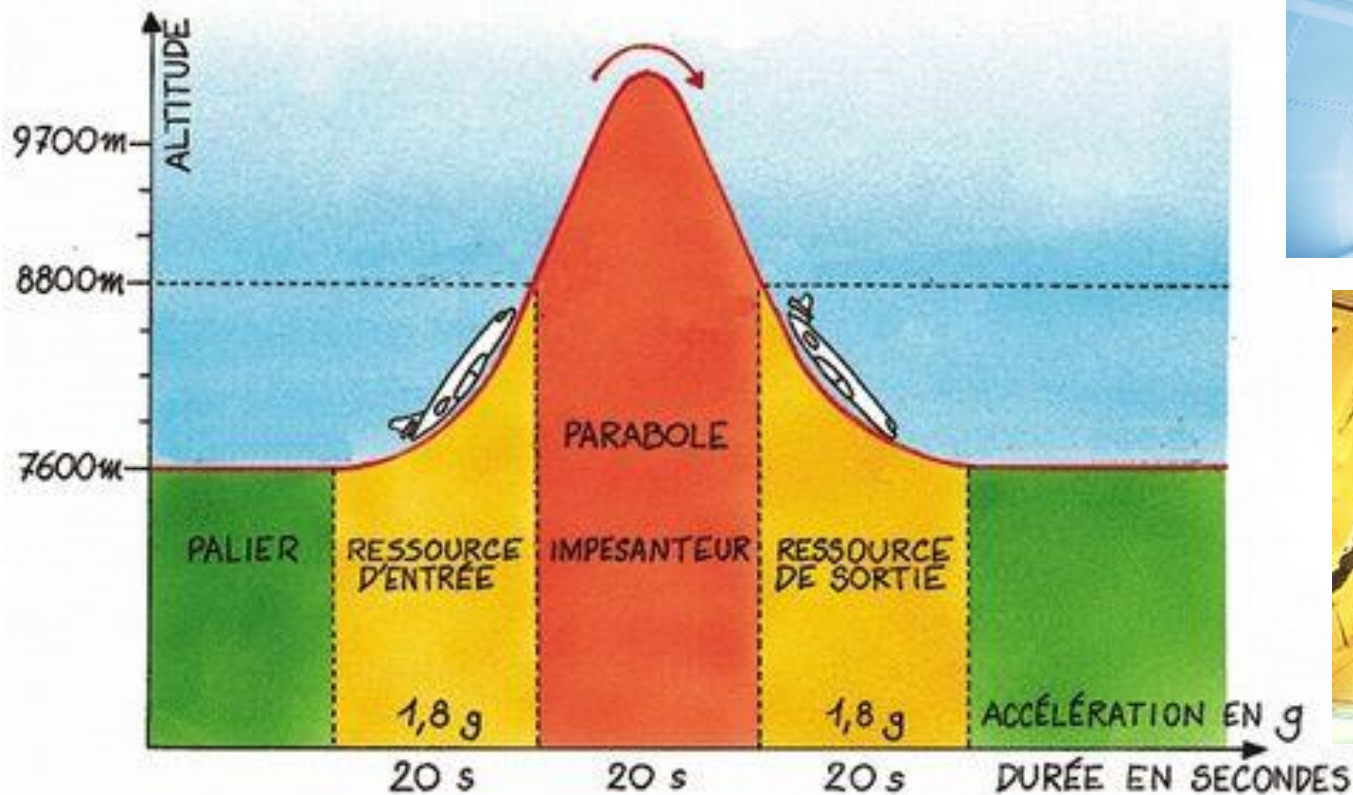
More details – next lecture...





# zero G parable

simulation of weightless stage (in an aircraft)



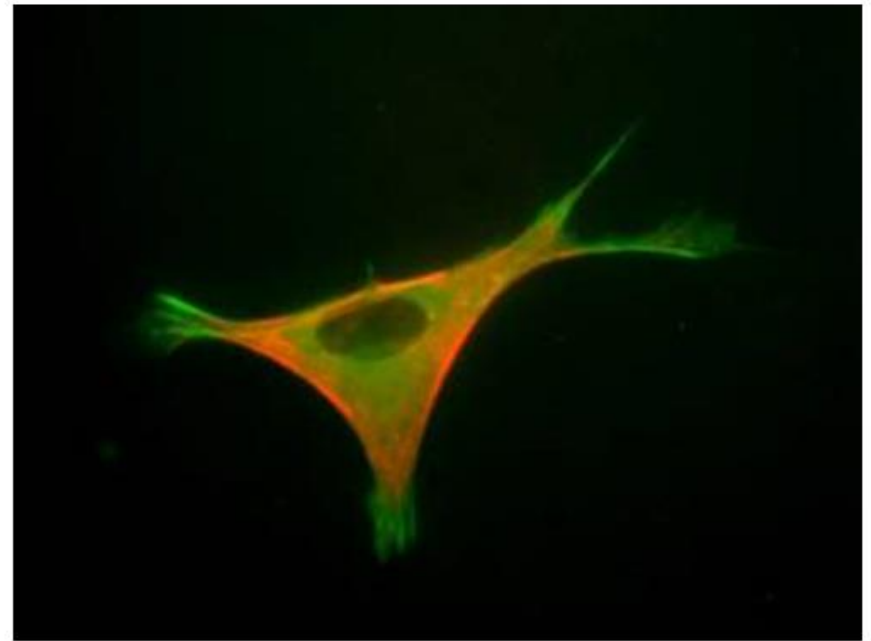
used also for commercial purposes:

<http://www.gozerog.com>

## Example: gravity and biology

Weightless stage – and its influence on muscles function

Muscle cells have unique ways of detecting mechanical stress. Scientists believe that the lack of mechanical stress on cells from gravity may decrease tension in the cell membrane and affect the expression of key proteins and genes, ultimately leading to muscle atrophy.



The type of mouse cell used in the Cell Mechanosensing investigation.

***Credits: JAXA/Nagoya University***